

# Measures of Angle Pairs

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# 7.4 Measures of Angle Pairs

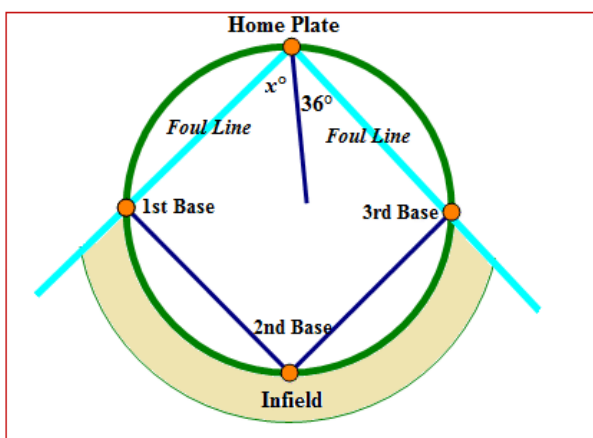
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[Figure 1]

The foul lines of a baseball diamond intersect at home plate to form a **right angle**. A baseball is hit from home plate and forms an **angle** of  $36^\circ$  with the third base foul line. What is the **measure** of the angle between the first base foul line and the path of the baseball?



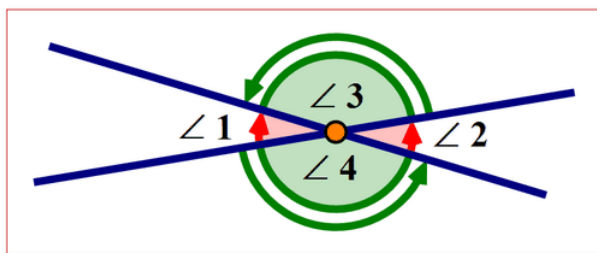
[Figure 2]

How can you use your knowledge of angles to figure out the measure of the angle?

In this concept, you will learn measure of angle pairs.

## Measuring Angle Pairs

There are different types of angle pairs. **Vertical angles** are an angle pair formed by **intersecting lines** such that they are never adjacent. They have a common **vertex** and never share a common side. Vertical angles are equal in measure. The following **diagram** shows vertical angle pairs.

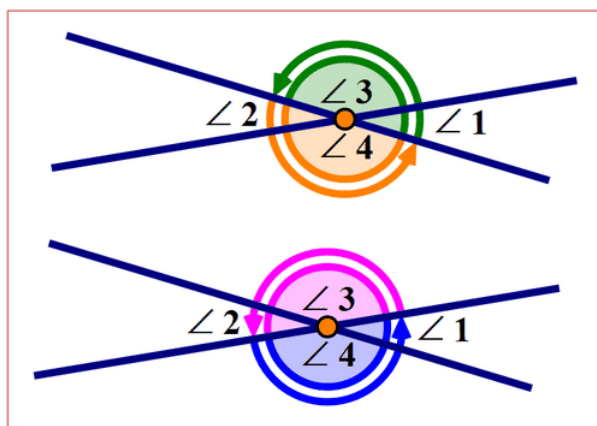


[Figure 3]

$\angle 1$  and  $\angle 2$  are vertical angles.  $m\angle 1 = m\angle 2$

$\angle 3$  and  $\angle 4$  are vertical angles.  $m\angle 3 = m\angle 4$

**Adjacent angles** are an angle pair also formed by two intersecting lines. **Adjacent angles** are side by side, have a common vertex and share a common side. The following diagram shows pairs of adjacent angles.



[Figure 4]

Each pair of adjacent angles forms a **straight angle**. Therefore the sum of any two adjacent angles equals  $180^\circ$ .

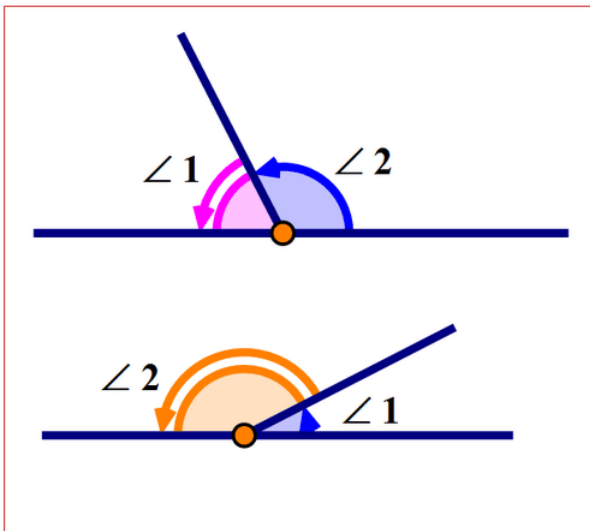
$$m\angle 1 + m\angle 3 = 180^\circ$$

$$m\angle 2 + m\angle 4 = 180^\circ$$

$$m\angle 2 + m\angle 3 = 180^\circ$$

$$m\angle 1 + m\angle 4 = 180^\circ$$

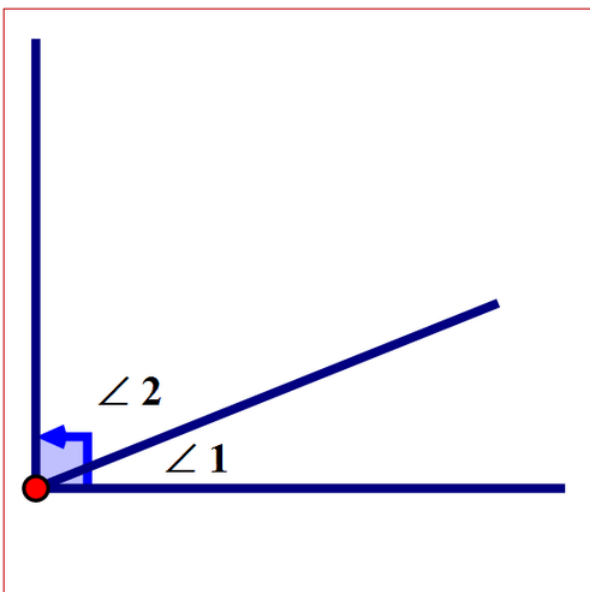
If the sum two angles is  $180^\circ$  then the angles are called **supplementary angles**. The following diagram shows two supplementary angles.



[Figure 5]

In both diagrams ,  $m\angle 1 + m\angle 2 = 180^\circ$  .

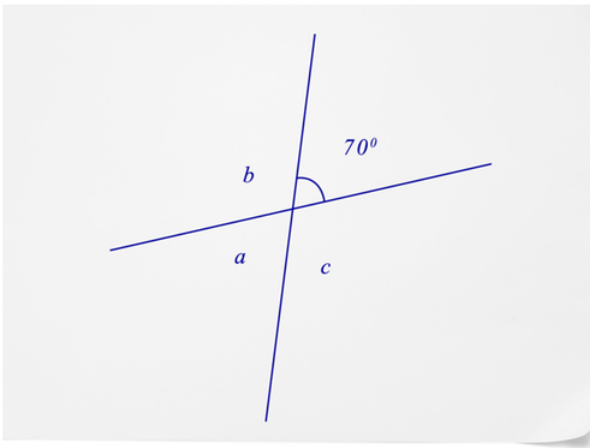
If the sum of two angles equals  $90^\circ$  then the angles are called **complementary angles**. The following diagram shows two complementary angles.



[Figure 6]

$$m\angle 1 + m\angle 2 = 90^\circ$$

Let's apply all this information about angles and their measure to determine the measure of  $\angle a$ ,  $\angle b$ ,  $\angle c$  in the following diagram.



[Figure 7]

There are four angles formed by intersecting lines. The measure of one of the angles is  $70^\circ$ .

First, state the relationship between the angle of  $70^\circ$  and  $\angle b$ .

The angle of  $70^\circ$  is adjacent to  $\angle b$  and the two angles form a straight angle.

Next, express the relationship using symbols.

$$\angle b + 70^\circ = 180^\circ$$

Next, subtract  $70^\circ$  from both sides of the equation.

$$\begin{aligned}\angle b + 70^\circ &= 180^\circ \\ \angle b + 70^\circ - 70^\circ &= 180^\circ - 70^\circ\end{aligned}$$

Then, simplify both sides of the equation.

$$\begin{aligned}\angle b + 70^\circ - 70^\circ &= 180^\circ - 70^\circ \\ \angle b &= 110^\circ\end{aligned}$$

The answer is  $110^\circ$ .

$$m\angle b = 110^\circ$$

First, state the relationship between the angle of  $70^\circ$  and  $\angle a$ .

The angle of  $70^\circ$  and  $\angle a$  are vertical angles and are equal in measure.

Next, express the relationship using symbols.

$$m\angle a = 70^\circ$$

The answer is  $70^\circ$ .

$$m\angle a = 70^\circ$$

First state the relationship between the angle of  $70^\circ$  and  $\angle c$ .

The angle of  $70^\circ$  is adjacent to  $\angle c$  and the two angles form a straight angle.

Next, express the relationship using symbols.

$$\angle c + 70^\circ = 180^\circ$$

Next, subtract  $70^\circ$  from both sides of the equation.

$$\begin{aligned}\angle c + 70^\circ &= 180^\circ \\ \angle c + 70^\circ - 70^\circ &= 180^\circ - 70^\circ\end{aligned}$$

Then, simplify both sides of the equation.

$$\begin{aligned}\angle c + 70^\circ - 70^\circ &= 180^\circ - 70^\circ \\ \angle c &= 110^\circ\end{aligned}$$

The answer is  $110^\circ$ .

$$m\angle c = 110^\circ$$

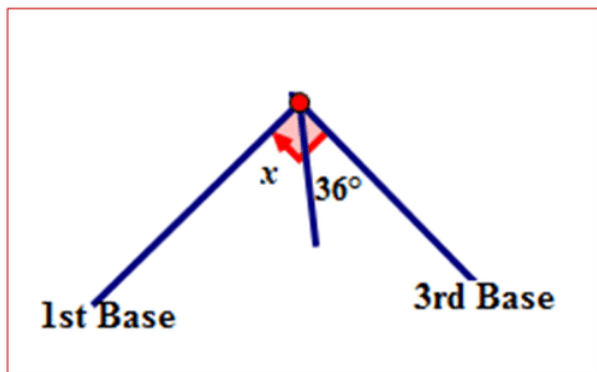
## Examples

### Example 1

Earlier, you were given a problem about the baseball field and the foul lines.

The angle between the path of the ball and the first base foul line needs to be figured out. This can be done using complementary angles.

First, draw a diagram to model the problem.



[Figure 8]

Next, state the relationship between  $36^\circ$  and  $\angle x$ .

$36^\circ$  and  $\angle x$  are complementary angles. The sum of the angles is  $90^\circ$ .

Next, express the relationship using symbols.

$$36^\circ + \angle x = 90^\circ$$

Next, subtract  $36^\circ$  from both sides of the equation.

$$\begin{aligned} 36^\circ + \angle x &= 90^\circ \\ 36^\circ - 36^\circ + \angle x &= 90^\circ - 36^\circ \end{aligned}$$

Then, simplify both sides of the equation.

$$\begin{aligned} 36^\circ - 36^\circ + \angle x &= 90^\circ - 36^\circ \\ \angle x &= 54^\circ \end{aligned}$$

The answer is  $54^\circ$ .

An angle of  $54^\circ$  is made between the first base foul line and the path of the baseball.

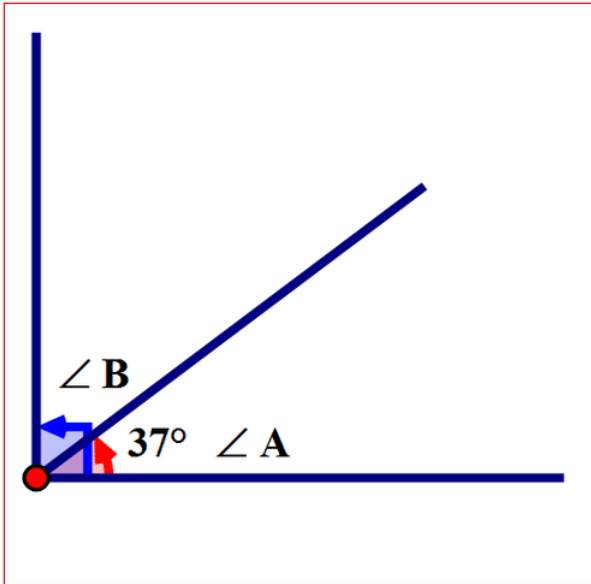
## Example 2



If the following angles are complementary, find the measure of the missing angle.

$$\angle A = 37^\circ \text{ then } \angle B = ?$$

First, draw a diagram to model the problem.



[Figure 9]

Next, state the relationship between  $\angle A$  and  $\angle B$ .

$\angle A$  and  $\angle B$  are complementary angles. The sum of the angles is  $90^\circ$ .

Next, express the relationship using symbols.

$$\angle A + \angle B = 90^\circ$$

Next, substitute the measure of  $\angle A$  into the equation.

$$37^\circ + \angle B = 90^\circ$$

Next, subtract  $37^\circ$  from both sides of the equation.

$$\begin{aligned} 37^\circ + \angle B &= 90^\circ \\ 37^\circ - 37^\circ + \angle B &= 90^\circ - 37^\circ \end{aligned}$$

Then, simplify both sides of the equation.

$$\begin{aligned} 37^\circ - 37^\circ + \angle B &= 90^\circ - 37^\circ \\ \angle B &= 53^\circ \end{aligned}$$

The answer is  $53^\circ$ .

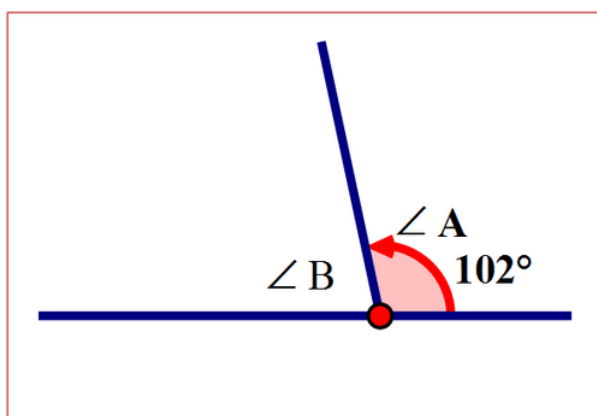
$$m\angle B = 53^\circ$$

### Example 3

If the following angles are supplementary, find the measure of the missing angle.

$$\angle A = 102^\circ \text{ then } \angle B = ?$$

First, draw a diagram to model the problem.



[Figure 10]

Next, state the relationship between  $\angle A$  and  $\angle B$ .

$\angle A$  and  $\angle B$  are supplementary angles. The sum of the angles is  $180^\circ$ .

Next, express the relationship using symbols.

$$\angle A + \angle B = 180^\circ$$

Next, substitute the measure of  $\angle A$  into the equation.

$$102^\circ + \angle B = 180^\circ$$

Next, subtract  $102^\circ$  from both sides of the equation.

$$\begin{aligned}102^\circ + \angle B &= 180^\circ \\102^\circ - 102^\circ + \angle B &= 180^\circ - 102^\circ\end{aligned}$$

Then, simplify both sides of the equation.

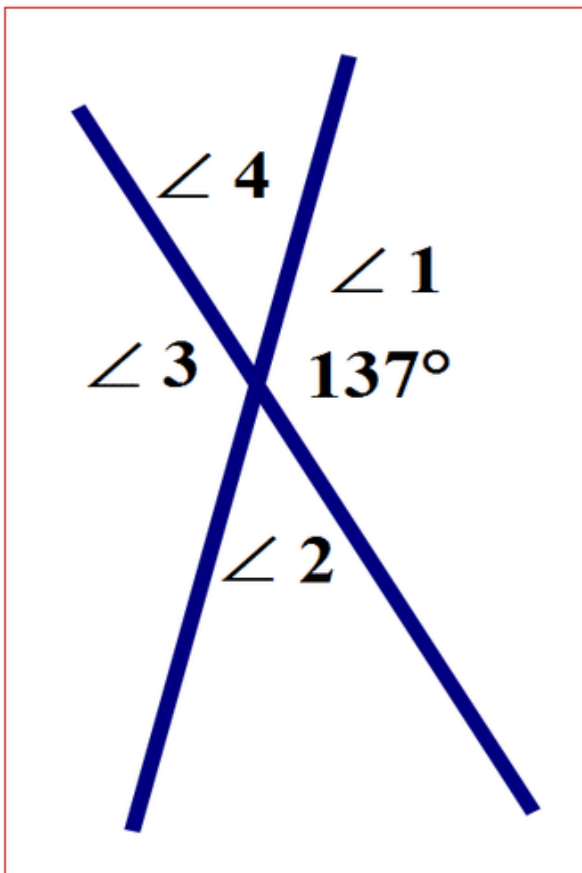
$$\begin{aligned}102^\circ - 102^\circ + \angle B &= 180^\circ - 102^\circ \\ \angle B &= 78^\circ\end{aligned}$$

The answer is  $78^\circ$ .

$$m\angle B = 78^\circ$$

#### Example 4

Using the following diagram, determine the measures of the missing angles.



[Figure 11]

First, state the relationship between the angle of  $\angle 1$  and  $\angle 3$ .

$\angle 1$  and  $\angle 3$  are vertical angles and are equal in measure.

Next, express the relationship using symbols.

$$m\angle 1 = m\angle 3$$

Next, substitute the measure of  $\angle 1$  into the equation.

$$\begin{aligned} m\angle 1 &= m\angle 3 \\ 137^\circ &= m\angle 3 \end{aligned}$$

The answer is  $137^\circ$ .

$$m\angle 3 = 137^\circ$$

First, state the relationship between the angle of  $\angle 1$  and  $\angle 2$ .

$\angle 1$  is adjacent to  $\angle 2$  and the two angles form a straight angle.

Next, express the relationship using symbols.

$$\angle 1 + \angle 2 = 180^\circ$$

Next, substitute the measure of  $\angle 1$  into the equation.

$$137^\circ + \angle 2 = 180^\circ$$

Next, subtract  $137^\circ$  from both sides of the equation.

$$\begin{aligned} 137^\circ + \angle 2 &= 180^\circ \\ 137^\circ - 137^\circ + \angle 2 &= 180^\circ - 137^\circ \end{aligned}$$

Then, simplify both sides of the equation.

$$\begin{aligned}137^\circ - 137^\circ + \angle 2 &= 180^\circ - 137^\circ \\ \angle 2 &= 43^\circ\end{aligned}$$

The answer is  $43^\circ$ .

$$m\angle 2 = 43^\circ$$

First, state the relationship between the angle of  $\angle 2$  and  $\angle 4$ .

$\angle 2$  and  $\angle 4$  are vertical angles and are equal in measure.

Next, express the relationship using symbols.

$$m\angle 2 = m\angle 4$$

Next, substitute the measure of  $\angle 2$  into the equation.

$$\begin{aligned}m\angle 2 &= m\angle 4 \\ 43^\circ &= m\angle 4\end{aligned}$$

The answer is  $43^\circ$ .

$$m\angle 4 = 43^\circ$$

## Review

If the following angle pairs are complementary, then what is the measure of the missing angle?

1. If  $\angle A = 45^\circ$  then  $\angle B = ?$
2. If  $\angle C = 83^\circ$  then  $\angle D = ?$
3. If  $\angle E = 33^\circ$  then  $\angle F = ?$
4. If  $\angle G = 53^\circ$  then  $\angle H = ?$

If the following angle pairs are supplementary, then what is the measure of the missing angle?

5. If  $\angle A = 40^\circ$  then  $\angle B = ?$
6. If  $\angle A = 75^\circ$  then  $\angle B = ?$
7. If  $\angle C = 110^\circ$  then  $\angle F = ?$
8. If  $\angle D = 125^\circ$  then  $\angle E = ?$
9. If  $\angle M = 10^\circ$  then  $\angle N = ?$
10. If  $\angle O = 157^\circ$  then  $\angle P = ?$

Define the following types of angle pairs.

11. Vertical angles
12. Adjacent angles
13. Complementary angles
14. Supplementary angles
15. Interior angles

## Review (Answers)

To see the review answers, return to the [Table of Contents](#) and select 'Other Versions' or 'Resources'.

## Resources

ck12.org

$(x+16)^\circ$   $(4x-5)^\circ$

Determine the measure of each angle.

$$\begin{aligned} x+16 &= 4x-5 \\ -x & \quad -x \\ \hline 16 &= 3x-5 \\ 21 &= 3x \\ \frac{21}{3} &= \frac{3x}{3} \rightarrow x=7 \end{aligned}$$


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